

Retention of ^{226}Ra by barite: the role of internal porosity

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Abstract

The role of internal macropores and nano-scale pores for the uptake of ^{226}Ra into barite was studied via scanning and transmission electron microscopy as well as focused ion beam methods. A temporal evolution of the internal microstructure and the Ra distribution was observed on samples taken from long-term Ra uptake experiments. The results of this study clearly show a significant impact of the presence of Ra leading to a complete reconstruction of the internal barite microstructure, whereas the microstructure of Ra-free reference samples remained unchanged. The initial internal barite microstructure contains a connected network

of macropores and a layered structure of nano-scale pores which, in the presence of Ra, coalesced in favor of larger pores during the experiment. A clear relationship between the Ra uptake and the internal porosity was observed by high-resolution STEM-EDX mappings. Starting from strongly enhanced Ra concentrations in the solid in the vicinity of the pores, Ra is temporarily inhomogeneously distributed within the barite particles. At later stages of the long-term experiment the Ra distribution becomes homogenous while nano-scale and macro-scale pores disappear. In conclusion, the uptake of Ra into barite takes place by a special case of dissolution/reprecipitation from the inside of the particle to the outside.

Keywords: Radium, barite, solid solution formation, dissolution/reprecipitation, nuclear waste management, electron microscopy, elemental mapping, FIB-SEM tomography

1. Introduction

The long-term fate of ^{226}Ra is of great environmental relevance due to its ubiquitous occurrence in the oil, gas and coal exploration and extraction and the resulting naturally occurring radioactive materials (NORM) (Varley et al., 2016; Attalah et al., 2015; Kondash et al., 2014; Rosenberg et al., 2014). Ra is one of the most important primary sources of elevated radioactivity created by industrial activity, energy production and mining. Coprecipitation and solid solution formation of Ra-phases with sparingly soluble sulfates, especially barite, leads to unwanted radioactive scale formation (Kondash et al., 2014; Al Attar et al., 2016).

Recently, the role of solid solution formation as an essential process for the remediation of contaminants was discussed (e.g. review of Prieto et al., 2016). In the case of Ra, the same mechanism which leads to unwanted radioactive scales is also applied to reduce the levels of Ra in the environment to legal standards, e.g. for the NORM removal from hydraulic

fracturing fluids. Therefore, the formation of the (Ba,Ra)SO₄ solid solution from high supersaturation has been intensively studied with respect to technical processes for the Ra removal (e.g. Stoica et al., 1998; Chalupnik et al., 2008). A recent review on the treatment of water contaminated with Ra poses the question of the long-term stability of the (Ba,Ra)SO₄ when disposed in lakes (IAEA, 2014). This open question still seems to hinder the application of (Ba,Ra)SO₄ co-precipitation for processing contaminated water.

Ra uptake at close-to-equilibrium conditions refers to the long-term behavior of Ra in the environment (Zhang et al., 2014; Rosenberg et al., 2011a, b). The special case of the contact between pre-existing barite and Ra in solution and their possible re-equilibration to a (Ba,Ra)SO₄ solid solution at close-to-equilibrium conditions has been a question of interest in several recent publications (e.g. Grandia et al., 2008; Bruno et al., 2007; Curti et al., 2010; Brandt et al., 2015; Torapava et al., 2014), because ²²⁶Ra is a key radionuclide in safety assessments of deep geological waste repositories for spent nuclear fuel. (Ba,Ra)SO₄ was recognized as possibly solubility limiting phase for Ra in the context of direct disposal of spent nuclear fuel. Based on thermodynamic considerations, uptake into pre-existing barite is predicted to be the main scavenger of Ra in several scenarios (Vinograd et al., 2013).

Recent experimental results demonstrated a complete recrystallization of pre-existing barite in the presence of Ra in time-scales of several hundred days (Bosbach et al., 2010; Curti et al., 2010). A detailed experimental study presenting repetitive long-term batch-recrystallization experiments was carried out by Brandt et al. (2015). This study provides an in-depth analysis of the solution chemistry, modelling of kinetics and thermodynamic data of the Ra uptake into barite based on a number of experiments conducted under carefully selected experimental parameters (solid/liquid ratio, grain size, and specific surface area).

A general trend of the temporal evolution of the Ra concentration in solution in such experiments is discussed in Brandt et al. (2015) and can be summarized by the following

three stages describing three different kinetic regions (Fig. 1), (1) slow initial decrease of the Ra concentration; (2) a faster decrease to a minimum Ra concentration below the predicted thermodynamic equilibrium (dashed line in Fig. 1) and (3) approach to thermodynamic equilibrium. The Ra-concentration in the solution is decreased by about 99.99 % of its initial value (Brandt et al., 2015).

Due to different onset times of the fast Ra decrease in solution, the concentration plateau was reached during a time interval of 600 to 1100 days (Brandt et al., 2015).

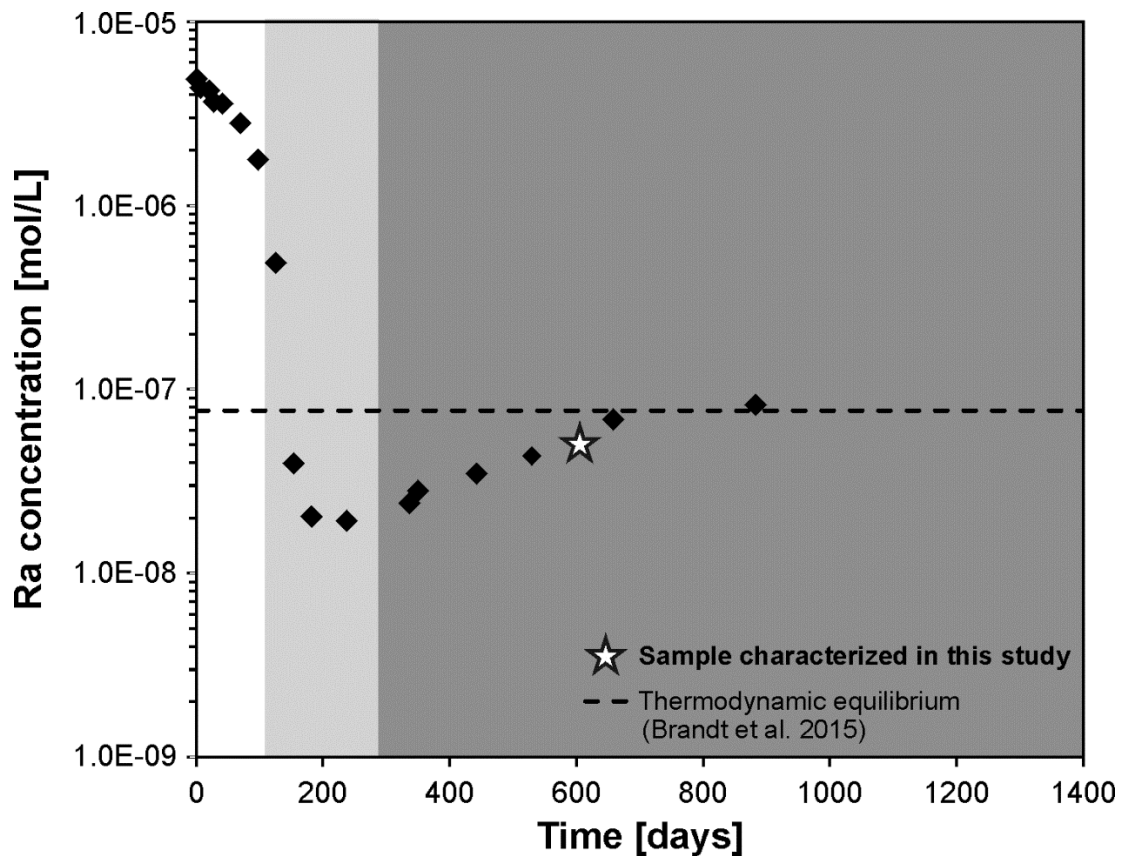


Fig. 1. Temporal evolution of the aqueous Ra concentration during a Ra uptake experiment as discussed by Brandt et al. (2015). The white area refers to stage 1, the light grey area to stage 2 and the dark grey area to stage 3 of the Ra-uptake. A sample from this experiment (★) was taken for comparison with an experiment carried out in the present study.

In order to gain fundamental insights into the uptake process, microscopic studies were conducted analyzing the barite morphology before and after the Ra uptake in comparison to Ra-free reference experiments (Klinkenberg et al., 2014). In this previous work, only very little changes of the outer shape and size of the barite particles were observed, leading to the conclusion that the uptake of Ra must be related to internal processes. The spatial resolution of the ToF-SIMS analysis provided in the same study allowed for the distinction between a surface layer and the Ra uptake into the crystal volume (Klinkenberg et al., 2014). Ra was clearly identified within the barite crystal volume. However, the pathways enabling the Ra uptake into barite and the temporal evolution of the Ra distribution within the newly formed solid-solution remained unclear. The studies of Brandt et al. (2015) and Klinkenberg et al. (2014) are forming the basis for the here presented results. As the study of Brandt et al. (2015) provides the complete and detailed description of the evolution of the Ra-concentration, the solution chemistry is only briefly covered here.

At ambient conditions, a replacement of pure barite by (Ba,Ra)SO₄ via solid state diffusion starting from the particle surface would be too slow for a complete exchange considering diffusion rates in minerals depicted e.g. in Zhang et al. (2008 and 2010). An alternative mechanism could be dissolution-reprecipitation, which has been recently studied extensively (e.g. reviews of Ruiz-Agudo et al., 2014; Altree-Williams et al., 2015). Despite the wide recognition of internal mineral phase exchange due to pseudomorphic replacement (e.g. Ruiz-Agudo et al., 2014; Altree-Williams et al., 2016; Putnis & Putnis, 2007; Hellmann et al., 2015), the underlying mechanisms remains not fully understood. The current understanding is that during a dissolution-reprecipitation process, a mineral phase AC consisting of a cation A and an anion C re-equilibrates due to a disequilibrium with another cation B in solution. This leads to the subsequent precipitation of the less soluble solid solution (A,B)C. For a complete

exchange, the interface between the solid and the aqueous solution needs to stay connected to the bulk fluid. Therefore, the newly precipitated phase needs to be porous.

The replacement of a parent mineral phase by a product phase is accompanied by changes in the overall porosity. Two main factors have an effect on this change in porosity. The first factor is the difference in the molar volume between the parent and the product phase. In addition, the second factor influencing the change in porosity is the solubility of the two phases (Putnis & Austrheim, 2013; Ruiz-Agudo et al., 2014). The solubility is determined by the grain size, fluid composition, temperature and pressure among other factors and will change during the replacement process. Large differences in solubility between parent phase (more soluble) and product phase (less soluble) might results in parent material loss during the reaction leading to an increased pore space in the product phase. Also, an increase in molar volume during replacement from the parent phase to the product phase can still result in a higher porosity. This was observed e.g. for the replacement of leucite by analcime (Putnis et al., 2007) or magnetite by pyrite (Qian et al., 2010). Furthermore, the strain which is related to high volume change reaction can induce fracturing which provides new pathways for fluid infiltration.

The change in porosity was defined by Pollock et al. (2011) not only regarding the molar volume but also the relative solubilities (Eq. 1):

$$V = 100 \times \left(\frac{n_p V_{m,p} - n_d V_{m,d}}{n_d V_{m,d}} \right) \quad (1)$$

Where n_d and n_p are the number of moles of the parent dissolved and the product precipitated and $V_{m,d}$ and $V_{m,p}$ are the molar volumes of the dissolving and precipitating phase respectively. For further references Altree-Williams et al. (2015) provide an extensive review on textural changes during mineral replacement by dissolution and reprecipitation.

The change in molar volume for the exchange of barite by a $Ba_xRa_{1-x}SO_4$ solid solution can

be estimated considering the change in molar volume by a complete replacement of barite by pure RaSO_4 first. Using equation (1), the change in molar volume can be calculated using the molar volumes of barite ($47.95 \text{ cm}^3/\text{mol}$) based on Hanor (2000) and a molar volume of pure RaSO_4 of $55.87 \text{ cm}^3/\text{mol}$ (Weigel & Trinkl, 1968). The precipitated and dissolved moles are set to one assuming complete replacement.

$$\Delta V = \left(\frac{1 \times 55.87 - 1 \times 47.95}{1 \times 55.87} \right) = 14.17 \% \quad (2)$$

Accordingly, the change in molar volume for the complete replacement of barite by pure RaSO_4 would be 14.17 %.

The solubility of barite is well studied over a range of temperatures and for this calculation, the solubility at ambient conditions provided by Blount (1977) of $\log K_{\text{BaSO}_4}$ of -9.97 is used. For RaSO_4 , the solubility constant implemented in the Nagra-PSI database (Thoenen et al., 2014) is $\log K_{\text{RaSO}_4} = -10.26$ as obtained by Langmuir and Riese (1985). Therefore, the difference in solubility between barite and RaSO_4 is less than 2.8 %.

A complete exchange of barite by radiobarite with a sufficient amount of Ra in solution would be expected to be accompanied by considerable microstructural changes. In contrast, the complete exchange with the relatively small amount of Ra provided in the experiments of Brandt et al. (2015) would be expected to lead only to minor microstructural changes.

The replacement process of mineral phase AC by a (A,B)C solid solution is based on the thermodynamic principle of energy minimization, yet this does not completely explain the kinetic driving forces. Only very little information is so far available about the kinetic driving forces controlling the mineral recrystallization and contaminant uptake relevant to the environment. Based on a detailed study of calcite, Ostwald ripening driven by surface energy minimization has been proposed as one important mechanism for recrystallization (Heberling et al., 2016). In a recent review about mineral recrystallization at low temperatures ($<100 \text{ }^\circ\text{C}$)

the importance of applying high resolution microscopy techniques has been emphasized to gain further insights into the molecular scale mechanism of stable mineral recrystallization (Gorski et al., 2016).

It is well known that natural barites often contain fluid inclusions entrapped during crystal growth (Böhlke & Irwin, 1992; Jamieson et al., 2016). Weber et al. (2016) characterized the fluid inclusions existing in barite which had earlier been used in the Ra uptake experiments of Curti et al. (2010), Klinkenberg et al. (2014) and Brandt et al. (2015). Nano-scale fluid inclusions filled with water and NaCl have been found to be arranged in layers by applying a complimentary approach of transmission electron microscopy (TEM) methods and atom probe tomography (ATP).

Here, we present a detailed electron microscopy and focused ion beam study addressing the temporal evolution of Ra uptake by pre-existing barite with a focus on the internal microstructure and the distribution of Ra during the different uptake stages. By applying TEM techniques in 2D in combination with a focused ion beam and scanning electron microscopy (FIB-SEM) analysis in three spatial dimensions on samples taken at different times of the Ra uptake, we provide essentially a four-dimensional description of the uptake process.

2. Materials and Methods

2.1 Barite samples from batch-type Ra uptake experiments

A batch type experiment was carried out with the aim of preparing samples for a detailed microscopic study of the temporal evolution of the internal microstructure of barite during Ra uptake. The setup of the batch-type recrystallization experiment was identical to that described in Klinkenberg et al. (2014). During the experiment, a synthetic high-purity barite (XR-HR-10) from Sachtleben Chemie® GmbH (SL barite) was put into contact with a

Ra-containing solution. The initial experimental conditions were a solid to liquid ratio of 0.5 g/L and a ^{226}Ra concentration in solution of $5 \cdot 10^{-6}$ mol/L. The concentration of ^{226}Ra in solution was analyzed using Gamma-Spectroscopy after filtering using a 10,000 Da Advantec ultrafilter.

Parallel to the sampling of the aqueous solution, solid samples were taken from each stage of the experiment and prepared on a Si-wafer after washing with iso-propanol for electron microscopy according to the procedure described in Klinkenberg et al. (2014). For comparison, a barite sample taken after 602 days from the experiment presented as SL 0.5 g/L in Brandt et al. (2015) was analyzed as well (Fig. 1). Reference experiments without Ra were carried out to separate the possible effects of recrystallization with and without Ra.

2.2 Characterization of the solids

2.2.1 FIB cross-section preparation and image analysis

Preparation procedures are described in detail in Weber et al. (2016) and in the references provided therein. Cross-sections along the longest particle axis were prepared by applying a variety of FIB instruments. Ra-containing samples were prepared in a Zeiss NVision40 cross beam workstation (Carl Zeiss AG, Germany) located in a controlled area, whereas Ra-free reference samples were prepared in two different but equivalent instruments, a FEI Helios NanoLab 460F1 (Kruth et al., 2016) or a FEI Helios Nanolab 400S (Meertens et al., 2016; FEI Company, The Netherlands).

The macropores within the barite samples were evaluated by the analysis of SEM images taken from FIB cross-sections. The areas comprising the complete particle and the areas corresponding to pores were separated and extracted by means of a contrast analysis (ImageJ) of the SEM images (Fig. 2). The area based macroporosity was calculated from the ratio of

the total particle and the macropore areas. A number of at least ten FIB cross-sections were prepared for this purpose and analyzed from each individual sample listed in Table 1.

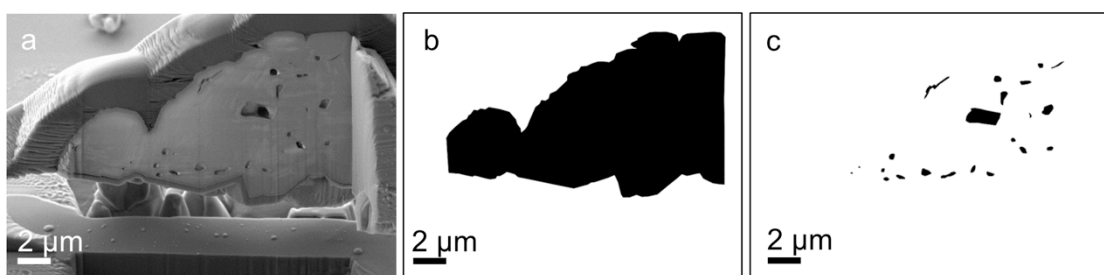


Fig. 2. Image analysis for the determination of the area based macroporosity: (a) SEM image of a barite particle FIB section, (b) extracted area of the barite particle, (c) extracted area of macropores

2.2.2 FIB-SEM tomography

FIB-SEM tomography with the slice & view technique (Holzer et al., 2004) was performed using a FEI Helios NanoLab 460F1 FIB-SEM instrument (FEI Company, The Netherlands; Kruth et al., 2016) to obtain the 3D visualization of the macropore distribution within the initial SL barite prior the addition of Ra. Slices of several barite particles were cut parallel to the longest particle axis and studied by SEM using secondary electron (SE) images. A 30 kV / 2.5 nA Ga ion beam was applied to cut two trenches on both sides of the particle and then a third trench from the front of the area of interest to expose the first segment of the slice-and-view section.

Tomographic data sets were acquired by sequential cutting of in total 734 slices of approximately 20 nm thickness with a 2.5nA ion beam and subsequent SEM. Each cross-section was imaged in mirror detection (MD) mode as well as by a through-the-lens back-scattered (TLD-BS) detector using a 2 kV/ 0.4 nA electron beam with a scan step size of 7.68 nm. The recorded SEM images were combined as a stack in a single three-dimensional volume by the tools available in the AVIZO 9.0.0 software package (FEI Company, The

Netherlands). Subsequently, the segmentation of the pore space was performed with the same software package.

2.2.3 TEM Sample preparation by focused ion beam (FIB)

TEM lamellae with a thickness below 100 nm were cut from the barite particles using a focused $^{69}\text{Ga}^+$ ion beam (FIB) instrument. The same variety of instruments as used for FIB cross-section preparation was used here. A detailed description of the barite sample preparation procedures applied in this study for particle cross-sections and cross-section TEM lamellae is given in Weber et al. (2016). A minimum of two TEM lamellae of each sampling date was prepared and thoroughly characterized.

2.2.4 Transmission electron microscopy (TEM)

A FEI Tecnai G² electron microscope (FEI Company, The Netherlands) (Luysberg et al., 2016) operated at 200 kV accelerating voltage was used to record selected area electron diffraction (SAED) patterns and scanning transmission electron microscopy (STEM) images using a high-angle annular dark-field (HAADF) detector.

Elemental maps were acquired by energy dispersive x-ray (EDX) mapping using a FEI Titan G² 80 – 200 electron microscope (Kovacs et al., 2016) equipped with an EDX system in the ChemiSTEMTM design (FEI Company, The Netherlands) operated at 80 kV accelerating voltage. The ChemiSTEMTM design consists of an annular orientation of four large-area, windowless SDD detectors in the Super-XTM geometry around the sample area, resulting in improved detection limits compared to the standard design.

3. Results and Discussion

3.1 Macroscopic results

The macroscopic results of the Ra-uptake experiment conducted in this study are displayed in Fig. 3 and summarized in Table 1. The macroscopic results obtained in this study are in good agreement with a large number of experiments discussed in detail in Brandt et al. (2015). In particular, these data sets indicate a Ra uptake of more than 99 % into the solid after stage 2, and the Ra concentration reaches a plateau in stage 3 (broken line in Fig. 3; Brandt et al., 2015), which was earlier discussed as approach to equilibrium between solid and solution. The Ra/Ba ratio after reaching equilibrium state is about $2 \cdot 10^{-3}$ and therefore, the molar volume change and the change in solubility associated with the replacement process can be considered negligible. As a conclusion, no internal microstructural changes would be expected based on the molar volume change or the difference of solubility between parent and resulting phase.

Several representative solid samples for further analyses were taken in order to follow the possible internal changes related to the stages of Ra-uptake: two samples in stage 1, one sample at the minimum Ra-concentration at stage 2 and two samples within stage 3. For comparison, a sample from the study of Brandt et al. (2015) taken at stage 3 was included in the analyses to make a direct link to this study and to the earlier study of Klinkenberg et al. (2014).

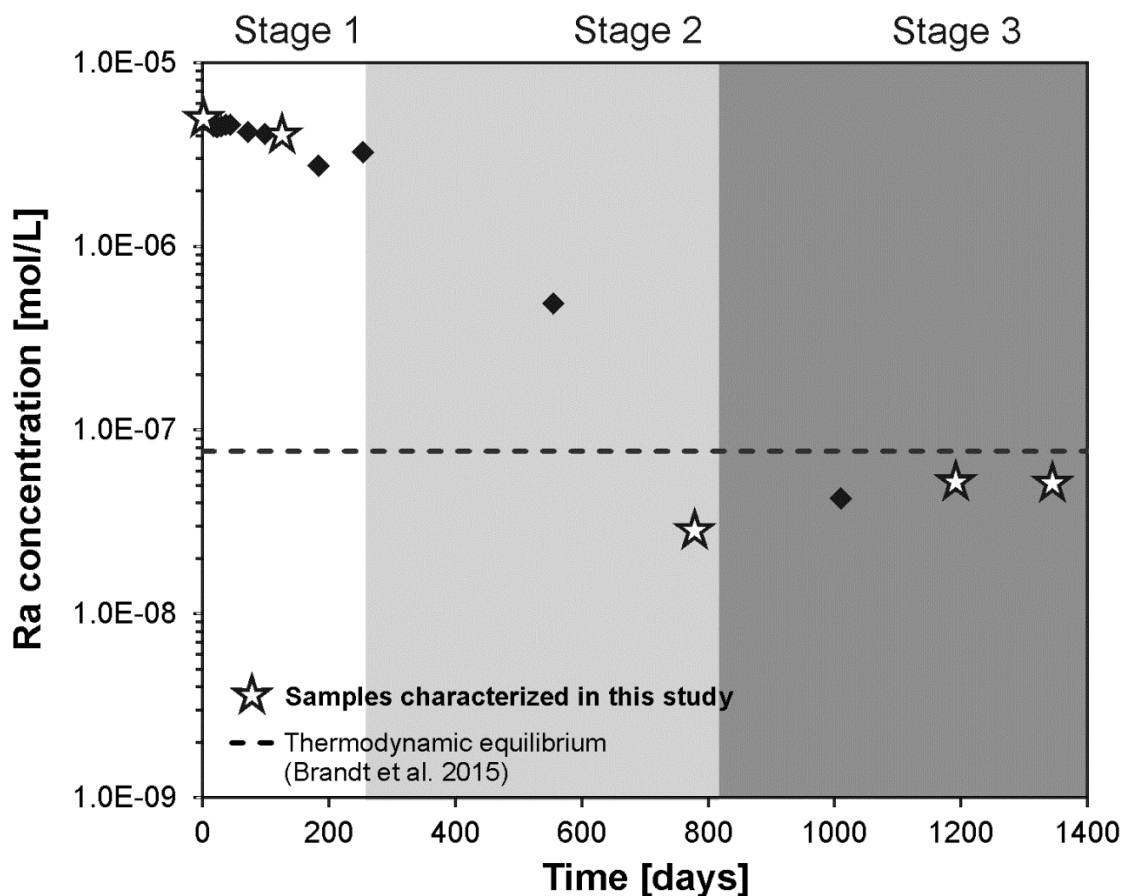


Fig. 3. Temporal evolution of the aqueous Ra concentration in the Ra-uptake experiment providing the samples for the microscopic study. Sampling of solid samples is marked with a \star . The thermodynamic equilibrium concentration was calculated using an interaction parameter of $a_0 = 1$ (Vinograd et al., 2013).

Table 1

Overview of solid samples from Ra uptake experiments and the Ra-free reference experiment. Experiment 2 was discussed in detail in Brandt et al. (2015) and Klinkenberg et al. (2014).

Sample	Experiment	Time [days]	Ra concentration in solution [mol/L]	Stage
Initial barite		0	0	0
Exp1_1a	Experiment 1	1	$4.90 \cdot 10^{-6}$	1
Exp1_1b	Experiment 1	126	$4.03 \cdot 10^{-6}$	1
Exp1_2	Experiment 1	779	$2.82 \cdot 10^{-8}$	2

Exp1_3a	Experiment 1	1192	$5.20 \cdot 10^{-8}$	3
Exp1_3b	Experiment 1	1345	$5.20 \cdot 10^{-8}$	3
Exp2_3	Experiment 2	602	$5.03 \cdot 10^{-8}$	3
Ref1	Reference 1	1	0	
Ref2	Reference 1	127	0	
Ref3	Reference 1	505	0	
Ref4	Reference 1	898	0	

3.2 Macro porosity and connectivity of pores and their temporal evolution of Ra-free reference samples

Numerous cross-sections of the initial barite were already prepared and discussed in Weber et al. (2016). The typical microstructure of this barite comprises macropores and nanometer scaled pores. Fast pathways for the uptake of Ra via pores would require a connection of pores and openings in the particle surface. However, so far the existence of an open pore network could not be shown based on single cross-sectional views. Therefore, FIB-SEM tomography was carried out here on an initial barite and on a grain of a reference experiment without radium after 127 days in solution. In contrast to individual FIB cross sections, the tomography technique provides a three-dimensional (3D) reconstruction of the macropore network as shown in Fig. 4. For example, Fig. 4a shows the SEM image of the initial SL barite particle and Fig. 4b the reconstructed particle based on the segmentation. Three pores in the barite surface are visible which indicate the presence of internal porosity with a connection to the outside. Typical for all initial barite samples analyzed by FIB cross-sections and tomography is a connected network of macropores (Fig. 4d) which is at least partially connected to the particle surfaces (Fig. Fig. 4c, orange circles). Compared to the particle volume, some of these pores provide a large entrance for Ra to enter from the aqueous phase by fluid diffusion and reach far into the inside of the particle. In some particles connected macropores were observed, opening up a significant reactive surface area in addition to the

outer particle surface. In addition to the figures presented here, a video of the 3D reconstruction is available in the supplemental information showing the three-dimensional distribution of the macroporosity.

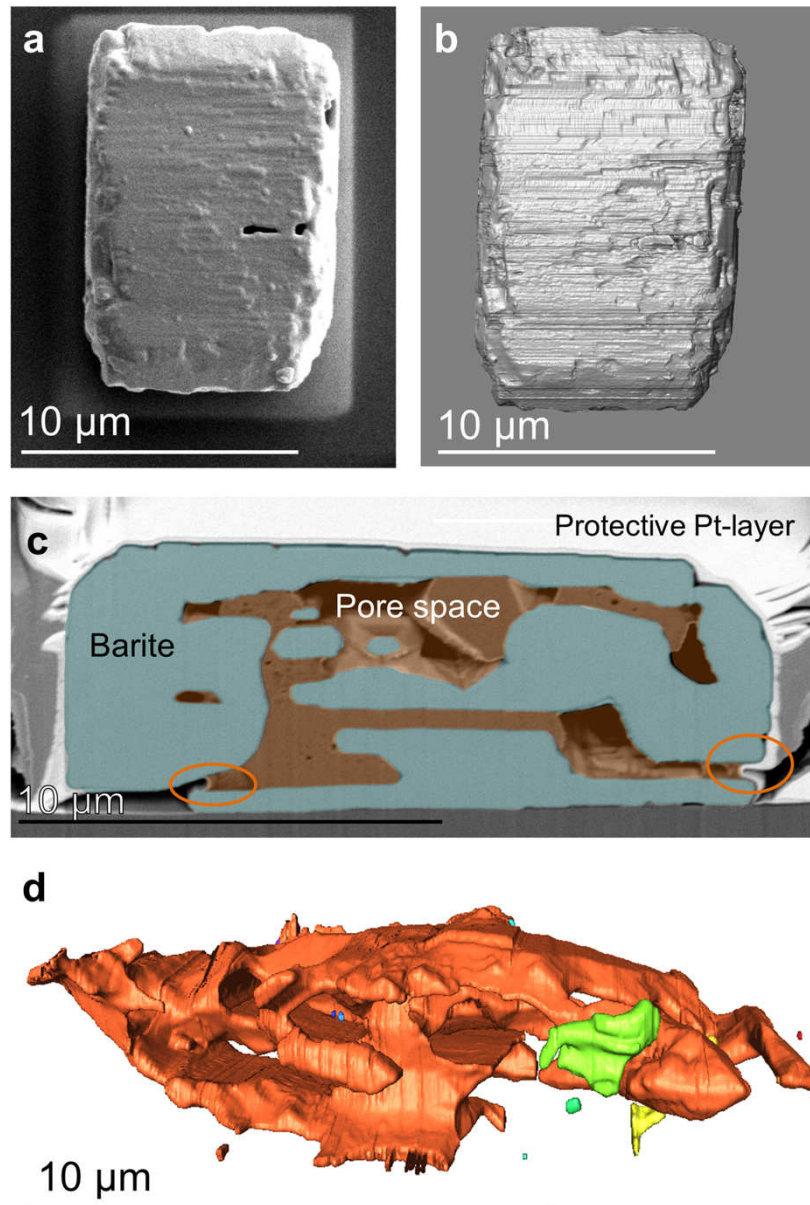


Fig. 4. FIB tomography of an initial SL barite particle: a) Top view SEM image of the SL barite particle. b) Top view of the reconstructed particle based on the segmentation of the outer material. c) Cross-section of the reconstructed volume showing the barite particle material selected for segmentation in blue and the selected pore space in orange. The orange circles highlight the open

macropores and the connection of the internal pores to the bulk fluid. d) Side view of the segmented pore volume. Connected macropores are highlighted in the same color.

Under the hypothesis that macropores are a possible pathway of Ra into barite via diffusion within the pore solution, an inhomogeneous uptake of Ra into barite would be expected owing to our observation that not all macropores are connected. Accordingly, the uptake may vary from particle to particle. Furthermore, it should be considered that one third of the 2D barite cross-sections did not show any porosity. In comparison to the initial sample, similar observations were made for the reference sample after 127 days. Connected macropores were observed in the FIB-SEM tomography of this sample as well, which were oriented mostly parallel to the outer surfaces of the particle (Fig. 5).

The evolution of the macroporosity was analyzed in detail by image analysis of FIB cross-sections from day 1, 127, 505 and 898 in order to identify whether the macroporosity inside the barite changes during recrystallization. The resulting area-based porosity is given in Table 2. No error is specified here as the determination is only semi-quantitative due to the limitations imposed by 2D cutting effects. Despite of these limitations, it should be still possible to observe a relative trend in the area-based porosity. However, the present data does not show a clear evolutionary trend of the porosity.



Fig. 5. FIB tomography reconstruction of a particle after equilibration in 0.1 mol/L NaCl for 127 days.

Table 2 Evolution of macroporosity inside Ra-free reference barite particles based on image analysis.

Sample	Time [days]	Number of analyzed cross-sections	Area-based porosity [%]
Ref1	1	11	1.5
Ref2	127	11	1.7
Ref3	505	5	2.3
Ref4	898	11	2.0

3.3 Temporal evolution of the nano-scaled pores in the Ra-free reference samples

In addition to the evolution of the macropores, nanometer scale pores were identified within barite samples taken at defined times during long-term experiments of up to 898 days (Fig. 6). Similar as described in Weber et al. (2016), SEM observations of the outside of all Ra-free reference samples (Fig. 6a,d) as well as the detailed observations in FIB cross-sections (Fig. 6b,e) and HAADF STEM images (Fig. 6c,f) indicate the presence of a layered structures formed by nano-scale pores. Dark HAADF STEM contrast indicate a high content of nano-scale porosity whereas bright areas indicate absence of nano-scale porosity. Within

898 days, the main change that was observed on the outside of the particles is a smoothening of the particle surfaces and a tendency of particles to merge. However, very little or no change of the internal microstructure was observed. Even after 898 days the layered internal structures are clearly visible (Fig. 6e, f). The width of the layered structures, their orientation and other characteristic features are very well comparable at all stages of the reference experiments. This can be taken as an indication of a very stable internal microstructure of barite. The high stability of fluid inclusions in barite was also recently reported by Jamieson et al. (2016) where they were proposed to preserve the conditions of physical and chemical processes at the seafloor. However, the same barite powders as used in the presented experiments appear to undergo significant recrystallization on the time scale of the experiment according to ^{133}Ba tracer experiments (Bosbach et al., 2010; Curti et al., 2010). Therefore, either the recrystallization in Bosbach et al. (2010) and Curti et al. (2010) may have been triggered by the presence of ^{133}Ba , or the fluid inclusions are stable against the recrystallization of barite itself.

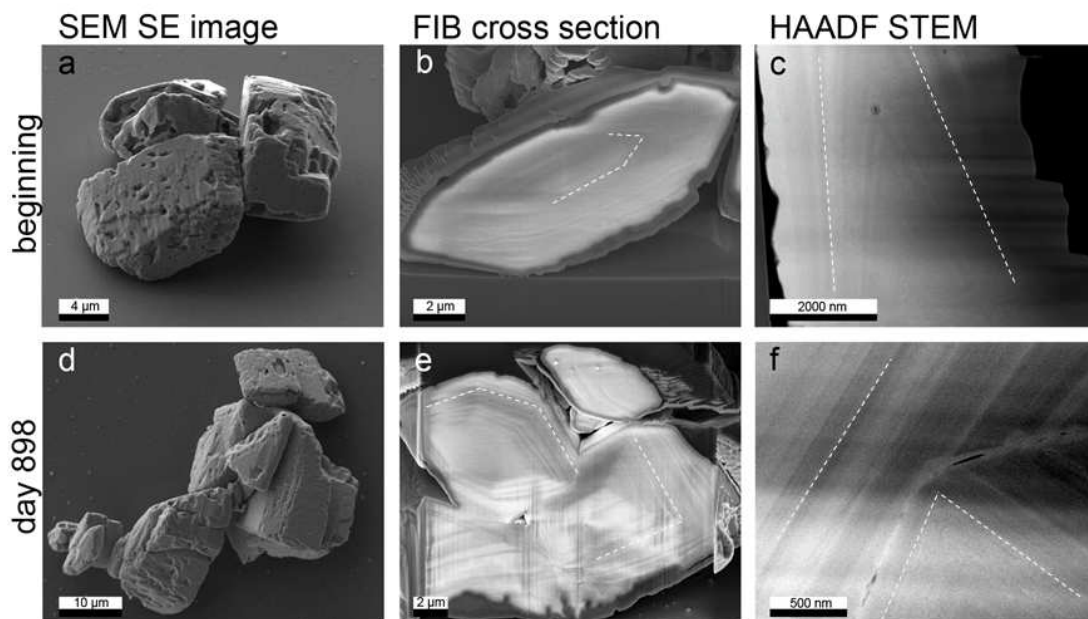


Fig. 6. Temporal evolution of the internal microstructure of SL barite from the Ra-free reference experiment at the beginning (a – c) and after 898 days (d – f). SEM images of the barite particles are given in (a) and (d), while (b) and (e) show SEM images of FIB cross-sections. The nano-scale porosity is visible as a layered structure in HAADF STEM images (c) and (f), where dashed lines trace back the layered structure.

3.4 Temporal evolution of barite samples from ^{226}Ra uptake experiments

During stage 1 no significant changes of the external microstructure could be detected by SEM imaging. At the middle of stage 1 (day 126), the surface of the barite particle in Fig. 7a shows many pores and a very irregular rough surface. The particles remained well separated.

At stage 2, the particles started growing together, forming chains (Fig. 7b). In most of the cases they were attached to each other either at the $\{210\}$ surfaces or at the $\{100\}$ surfaces. In a recently published study of Zhang et al. (2017), Van-der-Waals forces are considered as reason for crystallographic oriented attachment of particles. During the Ra uptake and barite recrystallization until stage 3, the barite surface is smoothened (Fig. 7c), and fewer pores than in the previous stages were observed. Later in stage 3, when approaching equilibrium, long

chains of particles have formed building a complex three-dimensional structure. In addition, the particles exhibit a further developed euhedral shape compared to the beginning of equilibration. Still large pores are visible in the barite particle surface as indicated in Fig. 7c.

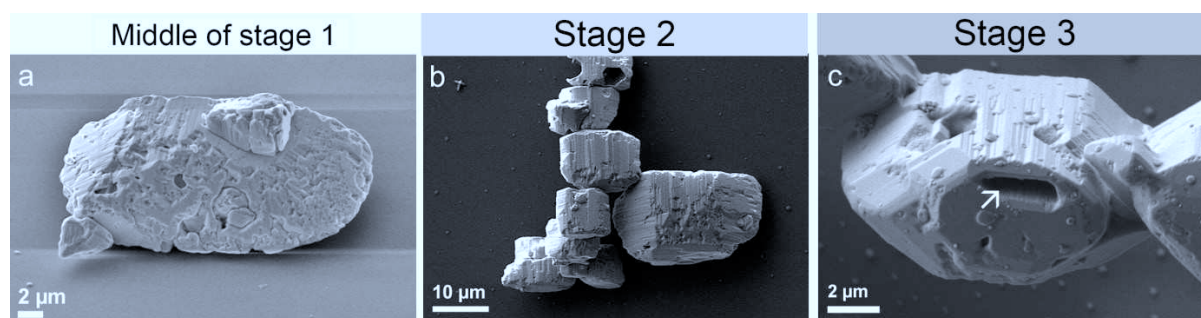


Fig. 7. SEM images showing the effects of recrystallization of barite in the presence of Ra. At the end of stage 1 (a), the crystal surfaces are very rough and many pores are visible. The Ra-barites start growing together and show a smoothing of the crystal surfaces at stage 2 (b). The particle shape evolves more towards euhedral barite shape. At the stage 3 (c), the Ra-barite particles are grown together. Crystal surfaces are smoother with new precipitates on them; the arrow indicates a pore.

Fig. 8 shows FIB cross-sections of radiobarites at different stages of the Ra-uptake. In the presence of Ra, the internal microstructure of the barite grains becomes instable and changes significantly already during stage 1 of the Ra uptake, while their external structure remains essentially unchanged. The internal microstructure now contains larger pores while the layered nano-scale pore structures are partially or even completely eliminated (Fig. 8c). In contrast to the Ra-free reference, the area-based macroporosity reaches a clear maximum in the middle of stage 1 (Table 3). This can be taken as an indication that the nanometer-scale pores coalesce to macropores during the Ra uptake, minimizing the surface free energy. The HAADF STEM images displayed in Fig. 9a-c shows the remaining layered structure consisting of nano-scale pores as well as of macropores in direct vicinity.

At stage 2, when the minimum Ra concentration in solution is reached, further coalescing of the nano-scaled pores has led to the formation of additional macropores and no layered structure could be observed in HAADF STEM and SEM images of FIB cross sections anymore (Fig. 8e,f; Fig. 9d-f). In comparison, even later in the reference experiment, layered structures are still clearly visible (Fig. 6e,f). The FIB section at this stage of the Ra uptake indicates that some of the pores are oriented in the same direction as the former layered structures whereas some are also irregularly distributed within the barite particles (Fig. 8e,f). The area-based macroporosity at this stage has decreased from ca. 6.6 % back to 3.7 % (Table 3). Additionally, as discussed in the later part of this study, the uptake of Ra and its heterogeneous distribution could be indicated by brighter contrasts in HAADF STEM images (Fig. 9d-f, Fig. 10).

During the final stage 3 of the Ra uptake experiments, macropores of several micrometers in length which are typically oriented parallel to the outer crystal surfaces occur in some of the FIB cross-sections (Fig. 8 g). In the HAADF STEM images an outer rim of higher density becomes visible, most likely indicating the formation of coherent newly formed (Ba,Ra)SO₄ (Fig. 9 h). Inside this rim, areas of increased nano-scale porosity are observed (Fig. 9 i). Additional HAADF STEM and TEM images showing this dense rim and the newly formed inner nano-scale porosity are given in the Fig. S1 and S2 of the supplemental information.

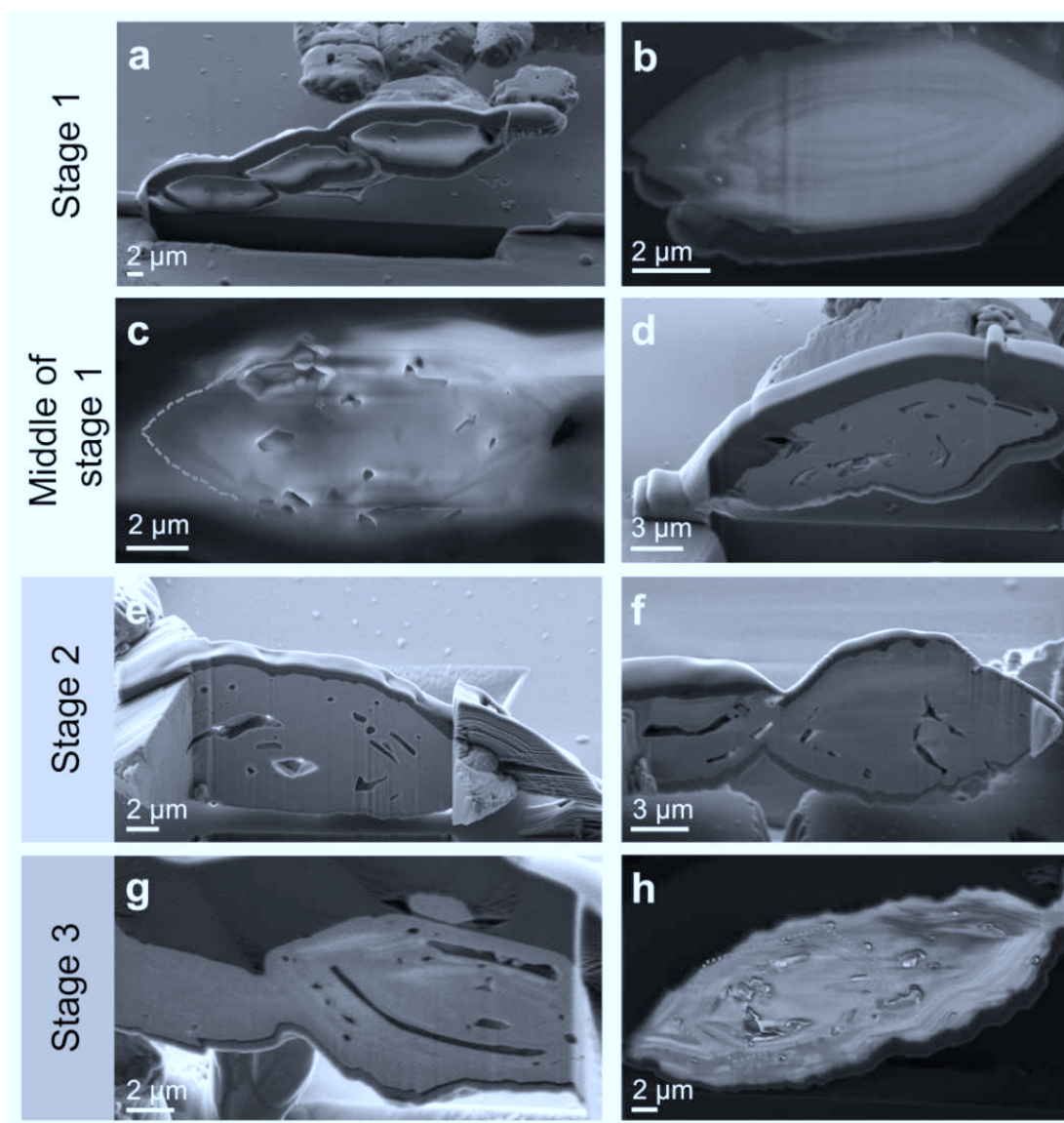


Fig. 8. FIB-cross sections of Ra-barites from different stages. In stage 1, particles with macropores (a) are present as well as particles with a layered structure (b). This layered structure starts to disappear in the middle of stage 1 (c) and more elongated pores can be observed (d). At stage 2, hollow barite cores are observed (e) as well as particles growing together (f). At stage 3, the macropores grow together (g) and particles are completely grown together to new particles (h).

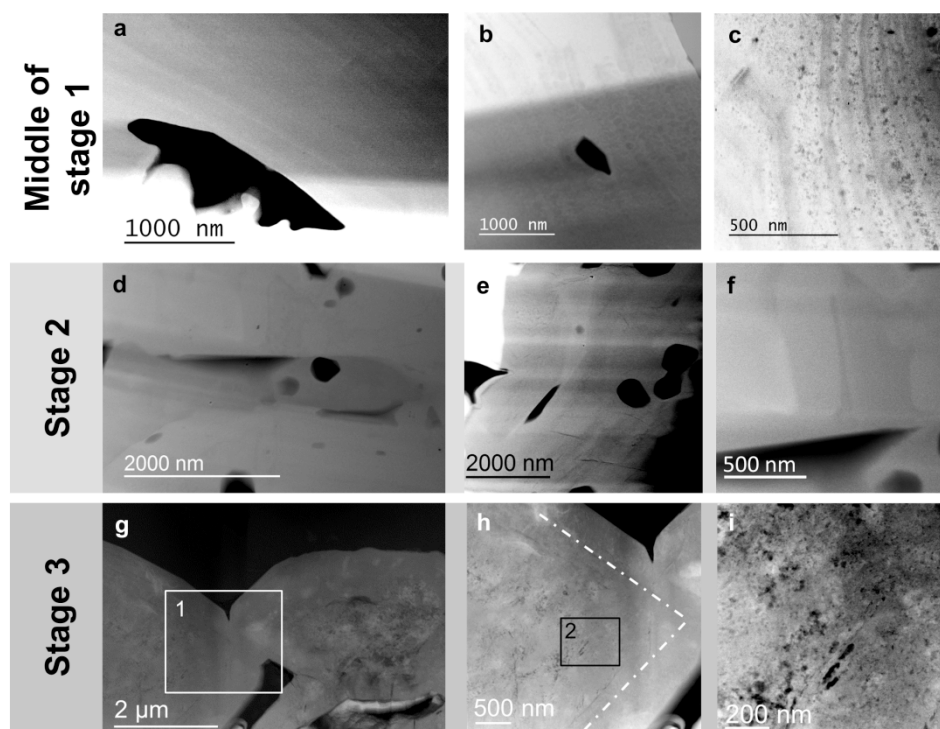


Fig. 9. HAADF STEM images of the Ra-barite sampled at different stages of recrystallization. The Ra-barites from the middle of the stage 1 clearly display a layered structure (a) and (b). At higher magnification (c), it is visible that the layers consist of larger nano-scale pores similar as observed in the beginning of stage 1. At stage 2, no layered structure can be observed anymore (d) – (f). Visible contrast variations could not be attributed to nano-scale porosity but could indicate an enrichment of Ra. At the stage 3 (g), a massive outer rim is visible. The area (1) is magnified in (h) showing this massive rim. The particles contain newly formed nano-scale porosity in the area (2) which is magnified in (i).

Table 3 Evolution of area-based macroporosity during Ra uptake based on semi-quantitative image analysis.

Sample	Stage	Number of analyzed cross sections	Area-based porosity [%]
Exp1_1a	1 beginning	9	3.5
Exp1_1b	1 middle	12	6.6
Exp1_2	2	4	3.7
Exp1_3	3	25	2.3

3.5 Temporal evolution of the spatial distribution of Ra

High resolution STEM-EDX measurements and mappings were performed to track the Ra uptake and (Ba,Ra)SO₄ solid-solution formation. No Ra was detected within FIB-lamellae of barite particles of sample Exp1_1b taken within the first half of stage 1 with STEM-EDX. Based on the Ra-concentration of the corresponding aqueous solution sample, only a very small amount of Ra should be present inside the barite sample at this stage. Since no Ra was detected by EDX spectroscopy, the Ra-concentration inside the barite solid is probably below the detection limit at the first half of stage 1. In contrast, Ra was clearly identified with the same technique in sample Exp1_2 taken at the time corresponding to the minimum Ra concentration in solution of stage 2 (Fig. 10). STEM-EDX mappings taken from the same sample indicate an inhomogeneous Ra and Ba distribution at this stage of the Ra uptake experiment (Fig. 10 b). The sample presented in Fig. 10a shows differences in the contrast indicating the presence of inhomogeneity. In this sample, the bright area is located between two pores. The EDX mapping shows a Ra distribution which qualitatively matches the HAADF contrast variations (Fig. 10b and c). A significant amount of Ra in the range of more than 1 at% is present in the yellow area of Fig. 11b. Higher Ra concentrations typically were observed near pores in the EDX mappings indicating that Ra appears to replace Ba (Fig. 11a).

Additional STEM-EDX mapping of samples from stage 2 demonstrating the inhomogeneous Ra distribution within the barite can be found in Fig. S3 - S5 of the supplemental information.

Fig. 11c shows the STEM-EDX mapping of the Ra containing sample at stage 3, corresponding to the approach of equilibrium between aqueous solution and solid. Based on mass balance between solid and solution and assuming a homogeneous distribution of Ra in the solid, the calculated Ra concentration of the barite particles was 60 ppm. Unfortunately, this is well below the detection limit of the applied EDX spectroscopy system. In the case of a homogeneous Ra distribution, consequently no Ra peak would be expected. The EDX spectrum corresponding to c confirms this expectation (Fig. 11d). Furthermore, the Ra-concentration in solution remained stable near the calculated equilibrium concentration during stage 3. Therefore, we deduce indirectly that Ra was distributed homogeneously in stage 3, i.e. a complete (Ra,Ba)SO₄ solid has formed, which is in equilibrium with the aqueous solution. Additional STEM-EDX measurements are given in Fig. S6 and S7 of the supplemental information.

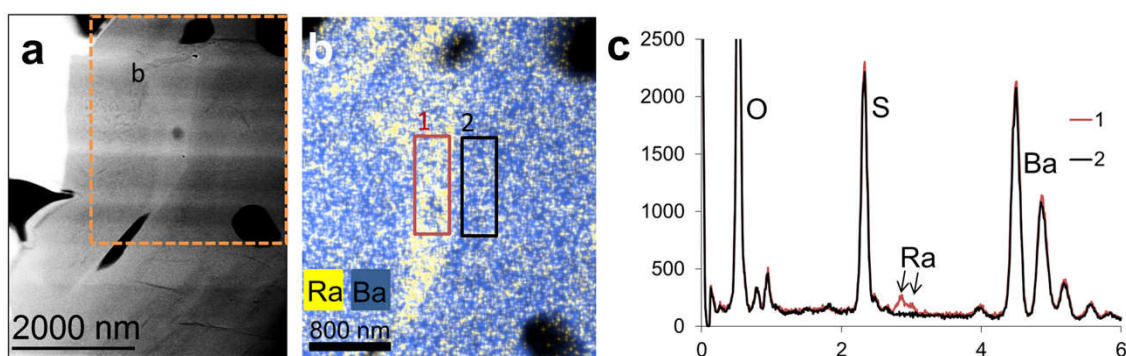


Fig. 10. Ra distribution inside the barite at stage 2. (a) HAADF-STEM image of sample Exp1_2 taken at stage 2, (b) corresponding STEM-EDX mapping of the area indicated in (a) by broken lines, (c) EDX-STEM spectra taken from the areas (1) and (2) in (b). The spectrum of area 1 shows clear signal of Ra, whereas no Ra signal is visible in spectrum 2.

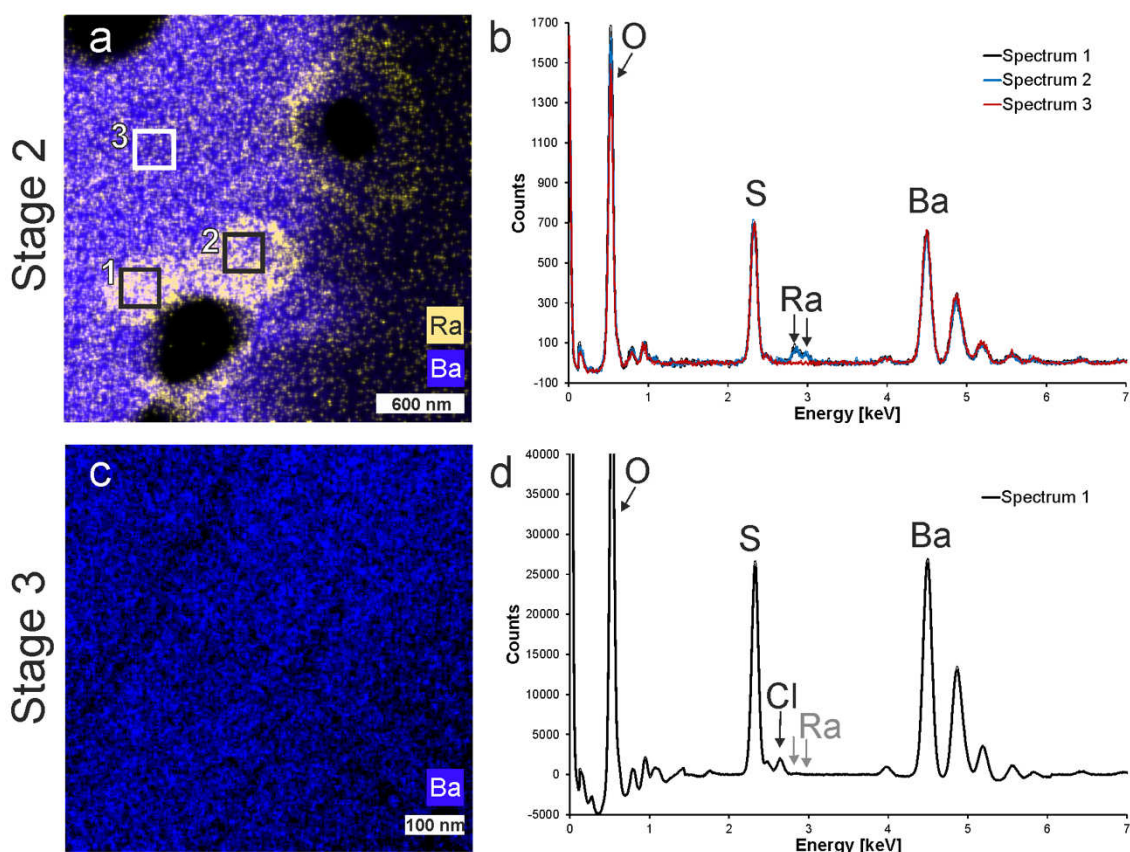


Fig. 11. Temporal evolution of the radium distribution from stage 2 to stage 3. (a) STEM-EDX mapping of Ra (yellow) and Ba (blue) at stage 2 (sample Exp1_2). The black areas are the macropores. (b) EDX spectra of the labeled areas 1, 2, and 3 (c) STEM-EDX mapping of barium stage 3 (sample Exp2_3) (d) corresponding EDX spectrum of the whole area, no Ra signal detected. The expected positions of the Ra-L peaks in the spectrum are marked by gray arrows.

4. Summary and conclusion

New insights into the mechanism of the Ra uptake into barite were obtained by comparing barite and Ra-barite samples applying a state-of-the-art high resolution microscopic approach. Characteristic for the initial barite sample was a connected macroporosity offering a fast pathway for Ra into the particle volume via fluid diffusion. The evolution of the

microstructure and the Ra distribution within barite was characterized at different stages of the Ra-uptake in order to understand the uptake mechanism.

In the presence of Ra, the surfaces of the barite samples became smoother with time, similar to the samples of the Ra-free recrystallization experiments. For the latter samples, also no significant changes were observed for the internal microstructure, even after recrystallization times of up to 898 days. In contrast to that, the overall porosity of the barite which was recrystallized in the presence of Ra changed in several steps: At the beginning, the nano-scale fluid inclusions disappeared, probably due to coalescing to new macropores, which could be favorable in the context of surface energy minimization. Later, the Ra-barite particles contained a dense rim structure with no porosity and an inner core of nano-scale porosity. In addition, the amount of macroporosity increased temporarily at stages 1 and 2, and was finally reduced again to a similar level as observed in the initial and reference samples. Energy minimization can be considered as a reason for reduction of macroporosity after the minimum observed in the radium concentration in solution. In addition, some available studies suggest that the reactivity of nanopores differs greatly from that of other pores (Stack, 2014, Stack, 2015). Therefore, the presence of nano-scaled fluid inclusions in the starting material could provide additional energy triggering the exchange process.

During stage 1, no Ra was detected in the solid by EDX spectroscopy. Ra may have migrated within the aqueous phase into the barite samples and may be still contained within the macropores. During stage 2, Ra was distributed inhomogeneously within the barite crystals. It was found to be concentrated in rims around some macropores. During stage 3, the Ra concentration was below the detection limit of EDX spectroscopy. A homogeneous Ra distribution in the particles and a stable aqueous Ra concentration support the conclusion that a thermodynamic equilibrium was reached at stage 3.

In summary, the mechanism of Ra uptake into barite appears to be a combination of Ra diffusion through macropores into the crystal volume and a dissolution-precipitation from the inside to the outside of the particles leading to a homogenous Ra distribution (Fig. 12). At the scale of the experiments, residual porous structures on the inside of the particles remain, although the solution composition approaches the predicted equilibrium of this solid-solution aqueous solution system.

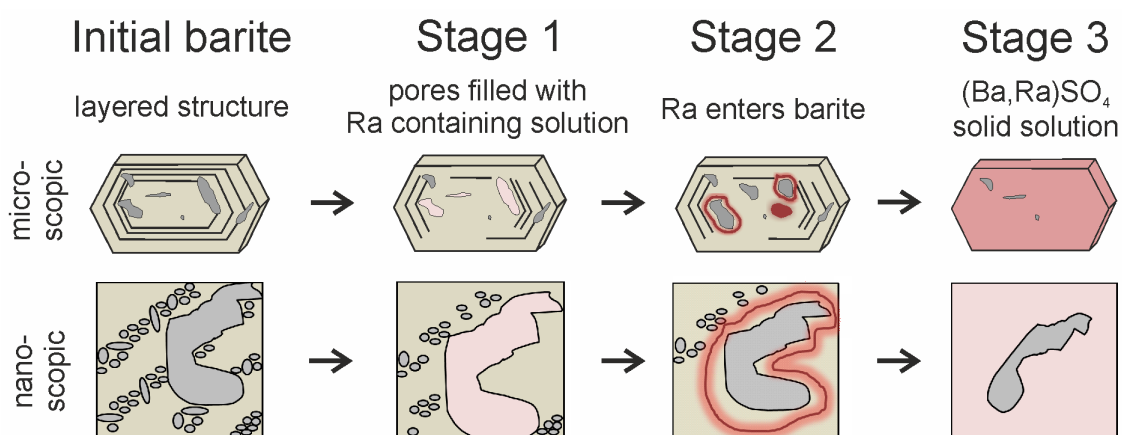


Fig. 12. Schematic summary of the process of Ra uptake into barite. Evolution of the micro/nano structure in the presence of Ra.

Our results indicate that barite can be destabilized and significantly reconstructed internally in the presence of a Ra-containing aqueous solution even though it appears to be quite stable and close-to-equilibrium from the outside. The reactivity of the barite powders containing fluid inclusions as investigated here could be utilized to directly remediate Ra from aqueous solution into a thermodynamically stable form or to stabilize (Ba,Ra)SO₄ precipitated via co-precipitation. The results also indicate that it is possible to take up more Ra into barite than thermodynamically stable, leading to inhomogeneities of the Ra concentration within barite particles. During the course of further equilibration, it can be expected that such (Ba,Ra)SO₄ solid solutions which may be formed via co-precipitation in contact with a Ra-free solution

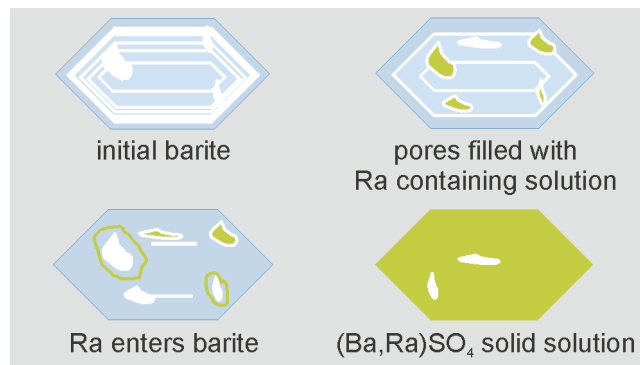
will release the surplus of Ra over a long time until equilibrium is reached. In this case, the addition of barite would keep the Ra in solution stable at a very low level.

Finally, regarding the implementation of the (Ba,Ra)SO₄ solid solution into safety assessments for deep geological disposal of spent nuclear fuel, the details of the Ra uptake in barite need to be understood. From the presented results, the attribution of the final steady state of the Ra concentration in solution to a homogeneous solid allows to take credit from this system.

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Graphical abstract



Highlights:

(maximum 125 characters, including spaces, per bullet point)

- Completely different evolution of the microstructure in Ra uptake and Ra-free recrystallization experiments observed
- Complete re-equilibration from a temporary, inhomogeneous Ra distribution to a homogeneous (Ba,Ra)SO₄ solid solution
- Uptake of Ra into barite by a special case of dissolution-reprecipitation process proceeding from the inside of the particle to the outside in addition to the uptake from the outside

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